

## ANALYSIS OF THE SOLAR STILL PRODUCTIVITY BY SIMILITUDE APPLICATIONS

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### ABSTRACT

*The aim of the present study is to develop mathematical analysis for common design solar still involving all ambient surrounding variables affecting its productivity and coefficient of performance. Two similar units of the solar stills were used namely: Control unit and cooled glass cover unit (cooled unit). The prediction equations for the productivity of the two studied units were reasonably accepted with coefficients of determinations ranged between 98-99%.*

*It was also found that the cooled unit has highest values of the productivity and coefficient of performance. The daily productivity and average coefficient of performance were 6.1655 kg/m<sup>2</sup>, 59.52% for the cooled unit compared to 5.536 kg/m<sup>2</sup> and 52.19% for the control unit.*

### INTRODUCTION

**F**rich and Sommerfeld (1973) designed a wick-type collector – evaporator or distiller of a shallow depth. They reported that it has a production rate of 3.8-4.4 L/m<sup>2</sup>.day, with an operational efficiency of about 40 to 46 %. Mostafa et. et. al. (1994) mentioned that the productivity of solar stills reaches its maximum value at an optimum cover slope. They added that the slope depends on the time of the year, the location of still, and the ambient conditions. An average slope of 20 to 25 degrees from the horizontal shows satisfactory results for a wide range of stills. Ernani (1996) studied a solar still versus solar evaporator. He concluded that, the distillation rate increases with increasing water temperature and temperature differences. Zabady (1997) mentioned that the total daily productivity decreases from 4646 to 4506, 4416 and 4323 cm<sup>3</sup>/m<sup>2</sup>.day with brine depth increased from 0.5 to 1.0, 1.5 and 2 cm respectively. The nocturnal production increased from 835 to 850, 900 and 912 cm<sup>3</sup>/m<sup>2</sup> when brine depth increased from 0.5 to 1.0, 1.5 and 2 cm respectively. Abdel-Rahman (2009) reported that at a maximum recorded

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value of solar intensity  $825 \text{ w/m}^2$ , and the corresponding air temperature of  $40.7 \text{ }^\circ\text{C}$ , the maximum and minimum solar still productivity and the corresponding transpiration rate accomplished in September were  $3196, 1910 \text{ g/m}^2$  and  $2234, 1254 \text{ g/m}^2$  respectively. Tayel et. al. (2009) designed and evaluated four different units of solar stills namely: control unit, preheated unit, air blowing unit and air suction unit. They studied several parameters affecting the productivity of the solar still as: brine depth, slope angle of glass cover, feeding water and covering materials. They reported that the preheating unit has the highest productivity ( $6030 \text{ cm}^3/\text{m}^2 \cdot \text{day}$ ) with brine depth of  $0.02 \text{ m}$ , slope angle of  $20^\circ$ .

### THEORITICAL APPROACH

The first step in the similitude application is to define the most associated variables affecting the phenomena under investigation. The following are the pertinent and independent variables considered to affect the productivity of the solar still. Their units and dimensions are as follows:

NO.	Symbol	Description	Dimension	Units
1	D	Productivity of the solar still	$\text{M L}^{-2} \text{ t}^{-1}$	$\text{kg/m}^2 \cdot \text{h}$
2	$\Delta P$	Evaporation and condensation potential or the difference between partial pressure at glass cover temperature and water temperatur	$\text{M L}^{-1} \text{ t}^{-2}$	$\text{kg m}^{-1} \text{ s}^{-2}$
3	$I_p$	Solar intesity	$\text{HL}^{-2} \text{ t}^{-1}$	$\text{W/m}^2$
4	$Q_{ec}$	Heat utilized in vaporizing water in the still	$\text{HL}^{-2} \text{ t}^{-1}$	$\text{W/m}^2$
5	$\Delta T_{g-a}$	Temperature difference between glass cover and the ambient air.	$\theta$	$^\circ\text{K}$
6	$U_L$	Over all heat loss coefficient	$\text{HL}^{-2} \text{ t}^{-1} \theta^{-1}$	$\text{W/m}^2 \text{ }^\circ\text{K}$
7	$\lambda$	Brine depth	L	m
8	$\phi$	Elapsed time	t	h
9	$\text{Cos } \beta$	Glass cover tilt angle	dimensionless	

The general relationship for the productivity of the solar still as a function of the associated independent variables can be expressed as:

$$D = F ( \Delta P , I_p , Q_{ec} , \Delta T , U_L , \lambda , \phi , \text{Cos } \beta ) \dots\dots\dots(1)$$

According to the Buckingham Pi-theorem, the number of dimensionless and independent quantities required to express a relationship among the variables in any phenomenon is equal to the number of quantities involved , minus the number of dimensions of those quantities Murphy (1950). In the present study nine quantities with five dimensions is involved. So, four dimensionless groups can be formed. The dimensional analysis yields the following relationship for both tested units:

$$\frac{\lambda D}{\Phi \Delta p (3600)^2} = \left[ A \left( \frac{Q_{ec}}{I_p} \right) + C \right] \cos \beta \dots\dots\dots(2)$$

Where A and C are functions of  $\pi_3$ . The value  $(3600)^2$  is used as conversion factor of  $\Delta p$  to  $\text{kg m}^{-1} \text{h}^{-2}$ . It is notable that  $\pi_2$  represents the C.O.P of the solar still.  $\pi_3 = [U_L \Delta T_{g-a} / I_p]$  represents the ratio between heat losses and solar insolation.  $\pi_1$  includes  $\Delta p$  that represents the potential of evaporation and condensation.  $\pi_4$  is a constant represents the view factor of sky, ground and surrounding with respect to cover tilt angle.

**MATERIALS AND METHODS**

In the present study two similar solar stills were used .The experimental part was carried out on the roof of the Agricultural Engineering Department Faculty of Agriculture Al-Azhar University Nacr City .

**Solar still construction:**

The solar still as shown in Fig.(1) is consists of an evaporator of four sides of galvanized iron sheet of 0.6 mm thick .The basin dimensions (evaporator) are 865x 695 mm, the still was insulated from its bottom and sides by two layers 0.03m f polyurethane and 0.016 m wood panels. The space above the basin is completely enclosed by a transparent cover tightly. The inside still base and sides are painted twice with a black paint. The outer surface of the glass cover for the cooled unit is surrounded by three sides of glass slices 30mm high, two ducts at the ends of the glass cover was made to allow cooling water to be easily collected and recycled. Saline water was distilled by the solar still and water was continuously fed.

## Measuring instrumentations:

**1 Thermocouples :** Temperature were measured using type-K

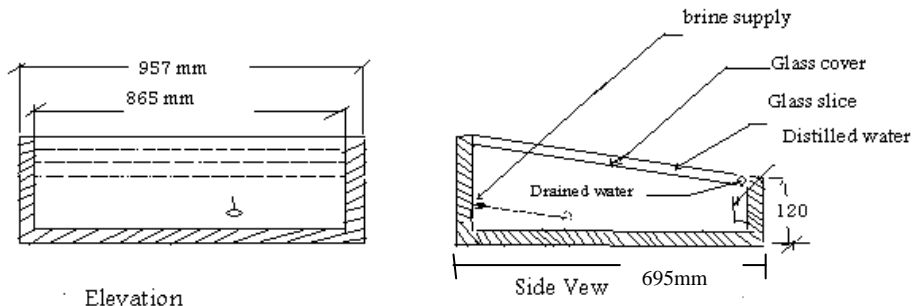


Fig.(1) Construction of the solar still (CGC unit).

thermocouples, the output device includes a large 4-digits temperature reading display and electronic circuitry, the specifications of thermocouples are manufactured in U.S.A, model 8528-40, full accuracy 18-28°C and useful range 4-45 °C

**2 Graduated glass bottle :**(1 liter) was used to measure the amount of distilled water.

**3 Solar intensity device:** A black and white pyranometer was constructed and tested by Ghanem (1989) and calibrated in the solar energy department, National research center, Giza Egypt. It was used for measuring the solar intensity in  $W/m^2$ .

**4 Turbo meter:** A turbo meter was used for measuring the wind speed in m/s, the meter is manufactured in U.S.A of measuring rang: 0 – 44.8 m/s.

## METHODS

### 1 Solar still energy balance

In the present work assuming steady state, the performance of the solar still can be described by energy balance that indicates conversion of the solar energy into useful energy gain, thermal losses and optical losses. The useful energy used in evaporation and condensation " $Q_{ec}$ " is equal to the difference between absorbed energy " $Q_{abs}$ " and energy losses. The thermal energy lost from the still to the surrounding by conduction, convection and infrared-radiation can be presented by the over-all heat

transfer coefficient "  $U_L$  " times difference of the average value of water and steel temperature "  $T_{ws}$  " and the ambient air temperature "  $T_a$  ". :

$$Q_{ec} = Q_{abs.} - U_L (T_{ws} - T_a) \dots\dots\dots(3)$$

**2 Over-all heat transfer coefficient of the solar still**

It is useful to develop the concept of over-all heat loss coefficient for the solar still to simplify the calculations. A thermal net work Fig.(2) was made to change the thermal loss in a similar electrical resistance around the basin to help in estimating the overall heat loss coefficient and the useful energy gain. Fig.(3) shows the equivalent thermal net work for the solar still. This method is considered the simplest one to evaluate the over-all heat loss coefficient for flat plate collectors as reported by Ria (1980) and applied by Shoukr et. al.(1986). The over-all heat transfer coefficient is the sum of top "  $U_T$  ", back "  $U_b$  "and edge "  $U_E$  "losses respectively which can be represented as:

$$U_L = U_T + U_b + U_E \dots\dots\dots(4)$$

**2-1 Top loss coefficient  $U_T$**

Energy losses through the top of the still is essentially a result of convection and radiation between the basin, cover plate, radiation and convection due to ambient air and sky temperatures.

**2-1-1 Basin loss coefficient  $R_1$**

The convection heat losses can be evaluated according to Rai(1980) as follows:

$$hc_{w-g} = 8.84 \times 10^{-4} \left[ (T_w - T_g) + \left( \frac{P_w - P_{wg}}{265 \times 10^3 - P_w} \right) (T_w + 273) \right]^{1/3} (P_w - P_{wg}) \dots\dots(5)$$

$$hr_{w-g} = \frac{0.9\sigma(T_w^4 - T_g^4)}{T_w - T_g} \dots\dots\dots(6)$$

Where

$hc_{w-g}$  : is the convection heat transfer coefficient between glass cover and brine water;  $W/m^2 \cdot K$ ,

$hr_{w-g}$  : is the radiation heat transfer coefficient between glass cover and brine water;  $W/m^2 \cdot K$ ,

$T_w$  : is brine water temperature; °K,

$T_g$  : is the glass cover temperature °K;

$P_w$  : is the partial pressure of water in  $P_a$  at  $T_w$  °C, .

$P_{wg}$  : is the partial pressure of water in  $P_a$  at  $T_g$  °C,

$\sigma$  : is Stefan Boltzman  $56.7 \times 10^{-9} \text{ W/m}^2\text{°K}^4$ .

Both partial pressures are evaluated by regressing steam table data for the partial pressure as a function of temperature at a range of 20-75 °C for the present study as follows:

$$P = 0.1483 T^3 - 8.4081T^2 + 341.34T - 2323.3 \quad (R^2 = 1) \dots\dots\dots (7)$$

Then, the loss resistance from the basin to the glass cover will be:

$$R_1 = \left( \frac{1}{hc_{w-g} + hr_{w-g}} \right) \dots\dots\dots (8)$$

**2-1-2 Glass cover loss to surrounding  $R_2$**

The resistance from the glass cover to surrounding due to the wind blowing and radiation " $hr_{g-a}$ "  $\text{W/m}^2\text{°K}$  can be determined according to Duffie and Bechman(1980) as follows:

$$hr_{g-a} = \epsilon_c \sigma ( T_g^2 + T_a^2 ) ( T_g + T_s ) \dots\dots\dots(9)$$

Where :

$\epsilon_g$  : is the emittance of the glass cover;0.9 ,

$T_s$  : is the sky absolute temperature °K ,

$T_a$  : is the ambient air temperature, °K ,

The wind losses " $h_w$ "  $\text{W/m}^2\text{°K}$  can be evaluated according to Rai(1980) :

$$h_w = 5.7 + 3.8 V_w \dots\dots\dots(10)$$

$$T_s = 0.0552 T_a^{1.5} \dots\dots\dots ..(11)$$

Then the top loss coefficient is:

$$U_T = \frac{1}{R_1 + R_2} = \left[ \frac{1}{(hc_{w-g} + hr_{w-g})} + \frac{1}{(hc_{g-a} + h_w)} \right]^{-1} \dots\dots\dots(12)$$

**2-2 Back loss coefficient  $U_b$**

The resistance to heat flow through the bottom of the steel pate is " $R_3$ " which is covered by insulation can be determined as follows:

$$R_3 = L_s / k_s \dots\dots\dots(13)$$

Where " $L_s=0.0006$  m" is the thickness of the steel sheet constructing the basin and " $k_s=48$ W/m<sup>o</sup>K" is the thermal conductivity of that sheet.

Duffie and Beckman (1980) reported that the bottom resistance is due to insulation.

**2-3 Resistance due to insulation**

The energy losses through the bottom of the solar still is represented by three resistances " $R_4$  ", " $R_5$  "and " $R_6$  ".  $R_4$  and  $R_5$  are resistances due to insulation and  $R_6$  is due to convection and radiation to the environment. Since  $R_4$  and  $R_5 \gg R_6$  we may neglect  $R_6$  in calculations of the bottom loss coefficient as reported by Rai(1980). So, back loss coefficient " $U_b$ " for the two layers of insulation, polyurethane and plywood of thickness and thermal conductivity of 0.03 m, 0.0245 W/m<sup>o</sup>K and 0.016m, 0.12 W/m<sup>o</sup>K respectively, can be determined as follows:

$$U_b = \frac{1}{R_b} = \frac{1}{(L_1/K_1)+(L_2/K_2)} \dots\dots (14)$$

**2-4 Edge loss coefficient  $U_E$**

Rai (1980) reported that if the edge insulation thickness is kept equal to the bottom insulation thickness, the edge losses may be estimated by assuming one dimensional sideway heat flow around perimeter of the still. Shoukr et.al.(1986) mentioned that the evaluation of edge losses is very complicated .However, in well designed system, the edge losses should be small that it is not necessary to predict it with great accuracy.

$$U_E = ( U A)_{edge} / A_s \dots\dots\dots(15)$$

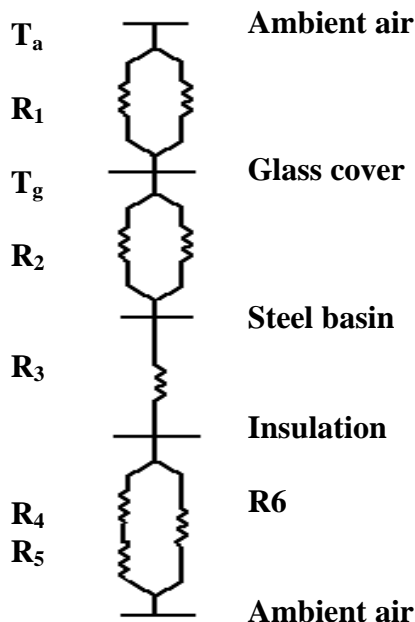


Fig.(2) Thermal net work of the still.

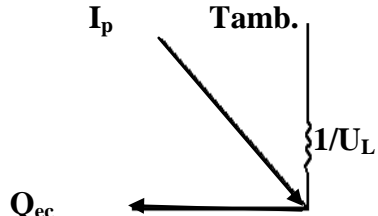


Fig.(3) Equivalent network.

Where ( **U A** ) **edge** is edge loss coefficient multiplied by its area m<sup>2</sup> and A<sub>s</sub> is the solar still area m<sup>2</sup>.

**3 Evaluation of heat flux by evaporation**

The rate of heat flux due to vaporizing water within the solar still "Q<sub>ec</sub> W/m<sup>2</sup>" can be determined according to Mostafa et.al. (1994) as follows:

$$Q_{ec} = 0.0061 \left[ (T_w - T_g) + \left( \frac{P_w - P_{wg}}{265 \times 10^3 - P_w} \right) (T_w + 273) \right]^{1/3} (P_w - P_{wg}) L_{HV} \dots\dots (16)$$

Where L<sub>HV</sub> is the latent heat of vaporization of water kJ/kg which can be evaluated by regressing steam table data for the latent heat of vaporization as a function of temperatures within the range of 20-75 °C in the present study as follows:

$$L_{HV} = -2.4124T + 2502.9 \quad (R^2=0.99) \dots\dots\dots (17)$$

To study the effect of glass cover temperature on the productivity and coefficient of performance of the solar still, two similar solar stills were constructed. One of them was used as a control unit and the other was cooled by spraying water three times per hour on the upper surface of the glass cover to reduce its temperature. Brine depth of 0.02 m and 20 ° tilt angle of the glass cover were used as reported by Tayel et. al.(2009). Solar intensity, ambient air, glass cover, steel basin, water in the tank and cooling water temperatures were hourly recorded. Wind speed was continuously recorded and average values were used.

**RESULTS AND DISCUSSIONS**

**3-1 Prediction equations :**

In the present study Table (1) and (2) summarize calculations for and π<sub>3</sub> for the cooled glass cover and control units. Figs.(4)and (5) showed justified relations between π<sub>1</sub>and π<sub>2</sub> at constant tilt angle of the glass cover i.e cos α = 0.9397, constant brine depth L= 0.02m and elapsed time of one hour, for the cooled cover and control unit of the form:

$$\frac{\lambda D}{\Phi \Delta P} = \left[ A \left( \frac{Q_{ec}}{I_P} \right) + C \right] \cos \beta \dots\dots\dots(18)$$

Where A and C parameters are functions of π<sub>3</sub>= [U<sub>L</sub>ΔT<sub>g-a</sub>/I<sub>P</sub>], Figs (6) shows the best fit relations, which are for the cooled unit:

$$A = 2.01 \times 10^{-14} \pi_3 + 4.475 \times 10^{-15} \quad (R^2=0.8) \dots\dots\dots(19)$$

$$C = 4.63 \times 10^{-12} \pi_3 + 6.17 \times 10^{-14} \quad (R^2=0.98) \dots\dots\dots(20)$$



And for the control unit :

$$A = -7.72 \times 10^{-15} \pi_3 + 1.39 \times 10^{-13} \quad (R^2=0.85) \dots\dots\dots(21)$$

$$C = 1.54 \times 10^{-12} \pi_3 + 1.543 \times 10^{-16} \quad (R^2=95) \dots\dots\dots(22)$$

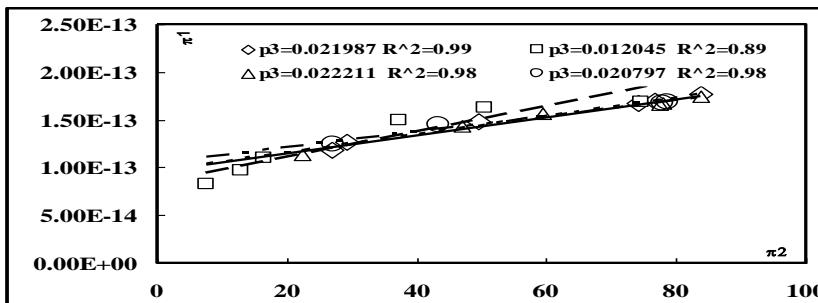


Fig.(4)Effect of  $\pi_2$  on  $\pi_1$  for the cooled unit.

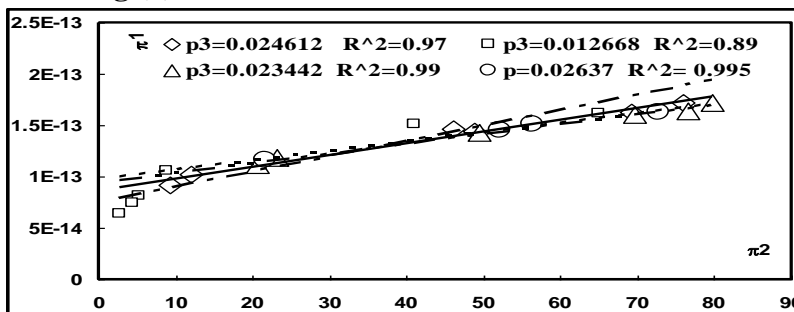


Fig.(5) Effect of  $\pi_2$  on  $\pi_1$  for the control unit.

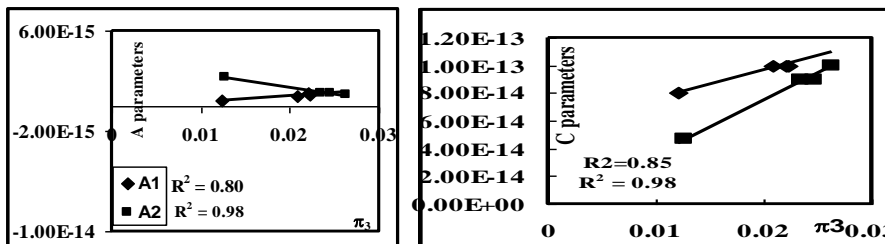


Fig (6)Evaluation of A and C parameters of the two studied units.

### 3-2 Productivity of the solar still

Prediction equation for determining the productivity of the cooled cover unit can be presented as follows:

$$D = \left[ 1.3 \times 10^{-5} \left( \frac{Q_{ec}}{I_p} \right) \left( \frac{U_L \Delta T_{g-a}}{I_p} \right) + 0.003 \left( \frac{U_L \Delta T_{g-a}}{I_p} \right) + 2.9 \times 10^{-6} \left( \frac{Q_{ec}}{I_p} \right) + 4 \times 10^{-4} \right] \Delta p \dots\dots\dots(23)$$

And for the control unit:

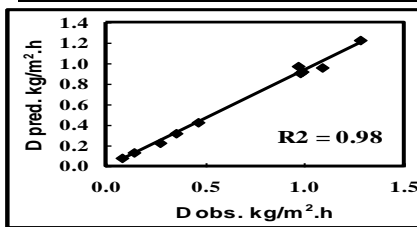
$$D = \left[ -5 \times 10^{-5} \left( \frac{Q_{ec}}{I_p} \right) \left( \frac{U_L \Delta T_{g-a}}{I_p} \right) + 10^{-3} \left( \frac{U_L \Delta T_{g-a}}{I_p} \right) + 9 \times 10^{-5} \left( \frac{Q_{ec}}{I_p} \right) + 10^{-7} \right] \Delta p \dots\dots\dots(24)$$

**Table (1) Evaluation of  $\pi_1, \pi_2$  and  $\pi_3$  for the cooled glass cover unit.**

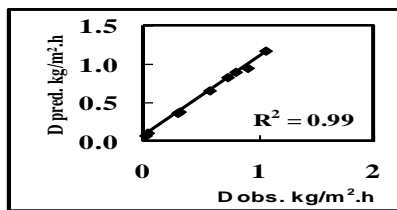
$I_P$	$\Delta T_{g-a}$	$Q_{ec}$	$\Delta P_{w-g}$	$U_L$	$\pi_1$	$\pi_2$	$\pi_3$
W/ m <sup>2</sup>	°K	W/ m <sup>2</sup>	P <sub>a</sub>	W/m <sup>2</sup> .°K	$\lambda D/\Delta p\phi$	$Q_{ec}/I_P$ %	$U_L \Delta T_{g-a}/I_P$
241	2.50	53.7	1074.2	1.02176	$1.14 \times 10^{-13}$	22.27	0.0106
320	7.74	150	2399.5	0.9874	$1.44 \times 10^{-13}$	46.95	0.0233
490	11.16	291	4244.9	0.9942	$1.57 \times 10^{-13}$	59.48	0.0226
770	19.27	596	8421.1	0.98582	$1.67 \times 10^{-13}$	77.44	0.0247
800	21.86	624	8835.6	0.98714	$1.67 \times 10^{-13}$	78.01	0.027
950	24.16	796	10840	0.89467	$1.75 \times 10^{-13}$	83.79	0.025
804	18.09	632	8838.3	0.98726	$1.69 \times 10^{-13}$	78.66	0.0222
765	19.18	596	8454.8	0.98769	$1.67 \times 10^{-13}$	77.97	0.0248
498	10.08	217	3440.7	0.99739	$1.44 \times 10^{-13}$	43.50	0.0202
315	5.10	85.4	1576.9	0.98963	$1.24 \times 10^{-13}$	27.10	0.016
Avg.						59.516	

**Table (2) Evaluation of  $\pi_1, \pi_2$  and  $\pi_3$  for the control unit.**

$I_P$	$\Delta T_{g-a}$	$Q_{ec}$	$\Delta P_{w-g}$	$U_L$	$\pi_1$	$\pi_2$	$\pi_3$
W/ m <sup>2</sup>	°K	W/ m <sup>2</sup>	P <sub>a</sub>	W/m <sup>2</sup> .° K	$\lambda D/\Delta p\phi$	$Q_{ec}/I_P$ %	$U_L \Delta T_{g-a}/I_P$
241	1.40	49.6	1016.5	1.0222	$1.11 \times 10^{-13}$	20.57	0.0059
320	2.55	74.2	1437.7	0.9887	$1.18 \times 10^{-13}$	23.19	0.0079
490	15.86	243	3925.7	0.9956	$1.43 \times 10^{-13}$	49.52	0.0322
770	24.27	536	7900.2	0.9866	$1.61 \times 10^{-13}$	69.56	0.0311
800	27.39	612	8847.9	0.9872	$1.64 \times 10^{-13}$	76.49	0.0338
950	28.66	757	10529	0.985	$1.72 \times 10^{-13}$	79.69	0.0297
804	24.09	584	8490.4	0.9879	$1.63 \times 10^{-13}$	72.69	0.0296
765	26.18	431	6765.5	0.9909	$1.51 \times 10^{-13}$	56.35	0.0339
498	15.18	259	4128.4	0.9953	$1.45 \times 10^{-13}$	52.05	0.0303
315	3.70	68.5	1344.5	0.99	$1.17 \times 10^{-13}$	21.75	0.0116
Avg.						52.185	



**Fig(7) Predicted and observed productivity for the cooled unit**



**Fig(8) Predicted and observed productivity for the control unit**

The observed and predicted productivities were evaluated and correlated to each other for the two tested units, Figs.(7) and (8). Prediction equations give reliable results for the still productivity of the two studied units. The coefficients of determinations were, 0.98 and 0.99 for the cooled and control units respectively. Table(3) shows that, as the solar intensity increases partial pressure potential  $\Delta P_{w-g}$ , glass cover, water

**Table(3) Solar intensity, glass cover temperature  $T_g$ , brine water temperature  $T_w$ , partial pressure potential  $\Delta P_{w-g}$  and productivity for the two studied units.**

Item	Cooled unit				Control			
	$T_g$ °C	$T_w$ °C	$\Delta P_{w-g}$ $P_a$	D $kg/m^2 \cdot h$	$T_g$ °C	$T_w$ °C	$\Delta P_{w-g}$ $P_a$	D $kg/m^2 \cdot h$
241	20.4	26	1074.2	0.0792	21.5	26.7	1016.5	0.0732
320	22.1	33	2399.5	0.2232	27.1	33.1	1437.7	0.1103
490	43	34	4244.9	0.4317	47.7	39	3925.7	0.3627
770	52	62	8421.1	0.9125	57	65.1	7900.2	0.8222
800	55.7	65	8835.6	0.9579	61.2	69	8847.9	0.9431
950	63	71.8	10840	1.2304	67.5	75	10529	1.1741
804	52.9	63.1	8838.3	0.9688	58.9	67	8490.4	0.8988
765	53	62.8	8454.8	0.9134	60	66.4	6765.5	0.6626
498	42.9	33	3440.7	0.3218	48	38.9	4128.4	0.3874
315	25	32	1576.9	0.1267	26.4	32.2	1344.5	0.1017
Avg.				6.1655				5.536

temperatures and productivity increases. The total daily productivity and average coefficient of performance were  $6.1655 kg/m^2$ , 59.52% for the cooled unit compared to  $5.536 kg/m^2$  and 52.19% for the control unit. The maximum productivity, water temperature, temperature difference between water and glass cover, and partial pressure potential of  $1.2304 kg/m^2 \cdot h$ ,  $71.8^\circ C$ ,  $8.8^\circ C$ , and  $10840 P_a$  for the cooled unit compared to  $1.0529 kg/m^2 \cdot h$ ,  $75^\circ C$ ,  $7.5^\circ C$  and  $10529 P_a$  for the control unit.

### SUMMARY AND CONCLUSION

The aim of the present study is to develop mathematical analysis for common design solar still involving all ambient surrounding variables affecting its productivity and coefficient of performance. Two similar units of the solar stills were used namely: Control unit and cooled glass cover unit (cooled unit). Similitude technique was used to develop prediction equations for these units. From the present study we can concluded that:

- 1- The prediction equations for the productivity of the two studied units were reasonably accepted with coefficients of determinations of 0.98 and 0.99 respectively. The predicted equations were of the form :

$$D = \left[ A \left( \frac{Q_{ec}}{I_p} \right) + C \right] (\Phi \Delta p) \frac{\cos \beta}{\lambda}$$

Where  $D$  is the productivity in  $\text{kg}/\text{m}^2\cdot\text{h}$ ,  $C$  and  $A$  are functions of  $\pi$  or  $[U_L \Delta T_{g-a}/I_p]$  which are linearly justified,  $\phi$  time duration in hours,  $I_p$  solar intensity  $\text{W}/\text{m}^2$ ,  $Q_{ec}$  the heat utilized in vaporizing water in the still  $\text{W}/\text{m}^2$ ,  $U_L$  over-all heat loss coefficient in  $\text{W}/\text{m}^2\text{K}$ ,  $T_{g-a}$ , temperature difference between ambient air and glass cover  $^\circ\text{K}$ ,  $\Delta P_{w-g}$  partial pressure potential  $\text{kg}/\text{m}\cdot\text{s}^2$ ,  $\lambda$  is a constant represents the view factor of sky, ground and surrounding with respect to cover tilt angle.

2- It was also found that the cooled unit has highest values of the productivity and coefficient of performance. The daily productivity and average coefficient of performance were  $6.1655 \text{ kg}/\text{m}^2$ , 59.52% for the cooled unit compared to  $5.536 \text{ kg}/\text{m}^2$  and 52.19% for the control unit.

3-The maximum productivity, water temperature, temperature difference between water and glass cover, and partial pressure potential of  $1.2304 \text{ kg}/\text{m}^2\cdot\text{h}$ ,  $71.8^\circ\text{C}$ ,  $8.8^\circ\text{C}$ , and  $10840 P_a$  for the cooled unit compared to  $1.0529 \text{ kg}/\text{m}^2\cdot\text{h}$ ,  $75^\circ\text{C}$ ,  $7.5^\circ\text{C}$  and  $10529 P_a$  for the control unit.

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### المخلص العربي

## تحليل انتاجية مقطر شمسي باستخدام التحليل البعدي

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نظراً لندرة المياه العذبة في بعض الأماكن الساحلية لجمهورية مصر العربية؛ يعد استخدام الطاقة الشمسية كمصدر للطاقة النظيفة والجديدة والمتجددة من افضل الطرق وأرخصها لتحلية مياه البحر. ويهدف البحث الى التوصل لنموذج رياضي يربط جميع المتغيرات المحيطة والداخلية بانتاجية مقطر شمسي ودراسة تأثير انخفاض درجة حرارة غطاؤه الشفاف ايضا على انتاجية واداءة . استخدم لذلك نموذجين متشابهين تصميميا حيث تم تبريد غطاء احدهم بالماء ثلاث مرات كل ساعة ومما سبق يمكننا استخلاص الأتي:

١. حققت المعادلات التي تم التوصل اليها نتائج مرضية في التنبأ بانتاجية كلا المقطرين موضع الدراسة حيث تراوح معامل الارتباط بين ٩٨% و ٩٩% وكانت صورة المعادلات:

$$D = \left[ A \left( \frac{Q_{ec}}{I_p} \right) + C \right] (\Phi \Delta p) \frac{\cos \beta}{\lambda}$$

حيث (D) هي الانتاجية كجم/م<sup>٢</sup> س، (A) و (C) تمثل دوال في المجموعة الثالثة  $[U_L \Delta T_{g-a} / I_p]$ ، (Q<sub>ec</sub>) هي الحرارة المستفاد بها في التبخير والتكثيف وات/م<sup>٢</sup>، (Φ) الزمن بالساعة، (ΔP) هو فرق الضغط الجزئي عند درجة حرارة المحلول الملحي والغطاء الزجاجي، (U<sub>L</sub>) هي معامل الفقد الحراري الكلي وات/م<sup>٢</sup> كلفن، (ΔT<sub>g-a</sub>) هي فرق درجات الحرارة بين المحلول الملحي والغطاء الزجاجي بالكلفن، (β) هي زاوية ميل الزجاج وهي ٢٠° و (λ) هي عمق المحلول في المقطر بالمتر.

٢. قدرت الانتاجية اليومية ومعدل الأداء بـ ٦,١٦٥٥ كجم/م<sup>٢</sup> و ٥٩,٥٢% للمقطر المبرد مقابل ٥,٥٣٦ كجم/م<sup>٢</sup> و ٥٢,١٩% لوحددة المقارنة.

٣. حققت أعلى انتاجية عند اعلى كمية اشعاع شمسي وعندما كانت درجة حرارة الماء المالح وفرق درجة حرارة بين سطح الزجاج والماء وكذلك فرق الضغط الجزئي ١,٢٣٠٤ كجم/م<sup>٢</sup> بس، ٧١,٨ م°، ٨,٨ م°، ١٠,٨٤٠ بسكال للمقطر المبرد مقابل ١,١٧٤١ كجم/م<sup>٢</sup> بس، ٧٥ م°، ٧,٥ م°، ١٠,٥٢٩ بسكال لوحددة المقارنة.

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