

DISSOLVED OXYGEN MASS BALANCE IN AQUACULTURE PONDS

SAMIR AHMAD ALI*

ABSTRACT:

The prediction of dissolved oxygen in aquaculture ponds throughout the year is essential to the design and evaluate the potential aquaculture sites. A computer model has been developed to simulate dissolved oxygen in a fish pond. A short-term Dissolved Oxygen (DO) fluctuation of a fishpond was developed by using various simple equations and continuous measurement of DO, temperature and solar intensity. Numerical computation has been performed for a typical winter (17th of January) and summer (17th of July) days.

Results from model verification runs showed that the model performance was satisfactory with respect to aquaculture pond dissolved oxygen. The relative percentage of error (RPE) for the 24 hours of simulation was 0.2818% and the correlation coefficient between predicted and measured dissolved oxygen was 0.97. The predicted dissolved oxygen was fluctuated between -0.101 to 0.113 gO₂m⁻³ lower and higher than the measured dissolved oxygen for most of the 24 hour simulation.

The predicted results indicate that DO is affected by weather variables, especially solar radiation. The dissolved oxygen (DO) values ranged from 4.4 to 8.7 g m⁻³, where it reached the highest value (8.7) at 17:00 h, while it reached the lowest value (4.4) at 6:00 h.

The fish growth model results indicated that the total cycle time between the stocking and the harvesting is about 180-190 days during the summer months; compared with the total cycle time in natural setting is about 210-240 days.

1. INTRODUCTION

Dissolved Oxygen (DO) is one of the most important factors affecting most aquaculture species. For fish culture, maintaining dissolved oxygen at a level suitable for fish survival and growth does pond management. When DO levels in aquaculture ponds become

*Agric. Eng. Dept., Fac. Agric., Moshtohor, Toukh, Qalubia, P.O. Box, 13736,
Egypt. Phone: +2 013 2467 034 Fax: +2 013 2467 78
E-Mail samir.ali@fagr.bu.edu.eg

low, the cultured organisms may become stressed or even die. A healthy balance pond provides a fluctuation in oxygen levels between day and night that leaves an adequate concentration of oxygen in the water that can support aquatic animal life during both day and night hours. Phytoplankton can exert a profound effect on water quality constituents, especially dissolved oxygen, by producing supersaturated concentrations during the day and reduced levels during the night due to biotic respiration and chemical oxidants result in a net loss of oxygen which can reach critically low concentrations (Muhammetoglu and Soyupak, 2000). The highest oxygen levels in a pond are usually measured on sunny afternoon when phytoplankton and other aquatic plants are producing oxygen through photosynthesis. The lowest level occurs just before daybreak after a night of oxygen consumption by aquatic plants and animals. Dissolved oxygen consumption and regeneration by phytoplankton is directly related to their rates of photosynthesis and respiration.

The intensity of solar radiation strongly regulates rates of photosynthesis and oxygen evolution in fishponds (Romaine and Boyd, 1979). The rate of oxygen production is a function of the concentration of algae and other forcing functions. Because the growth of algae is light and temperature dependent, hence the rate of photosynthetic oxygen production follows the same pattern. Temperature is a parameter that shows a marked seasonal and daily variation in fishponds. It influences photosynthesis, growth of algae and bio decomposition of organic matter in the pond. Other factors such as density of fish, turbidity, organic matter levels and wind velocity also greatly influence dissolved oxygen budgets for fishponds (Boyd *et al.*, 1978). In ponds showing marked stratification, surface waters may be harmful to fish due to supersaturated DO conditions in combination with high temperatures, while in the same pond near anoxic conditions may exist close to the bottom (Chang and Ouyang, 1988; Losordo, 1988; Boyd, 1990).

There are several reports of DO models incorporating mechanistic characterization of the chemical, physical and biological processes in an open pond which governs the resulting DO levels (Losordo, 1988; Losordo and Piedrahita, 1991). The intent of the present study describes

to develop a dissolved oxygen model using input variables in low cost greenhouse fishpond. In this study additional modification have been implemented to the predictions of DO performance in greenhouse fishpond from calculation of solar radiation falling on greenhouse canopy cover to the pond water surface. This model simulates the hourly variation of DO in a fishpond over a 24 h period as influenced by the consumption and production of oxygen by phytoplankton and fish. Measurable rates of photosynthesis and respiration are needed for proper calibration of the model. This model is neither site nor species specific and input variables can be adjusted to accommodate most pond conditions. In freshwater fishponds effects of solar radiation on temperature and oxygen variations have been described in detail (Boyd, 1979). The model was developed with the following objectives under consideration:

- To determine components which have greatest effect on DO.
- To predict the DO concentration in aquaculture ponds.

2. Model Development.

2.1. Dissolved oxygen model.

The modeling of dissolved oxygen concentrations in an aquaculture pond depend upon some factors, which contributes oxygen entry into the pond, oxygen removal from the pond and oxygen exchanges within the pond. In a pond, dissolved oxygen concentrations depends on the balance between photosynthetic production, total respiration and exchanges with atmosphere (Eq. 2).

Two main hypotheses of the DO models are as follows:

- It is assumed that pond water is completely mixed.
- Biomasses and nutrients are supposed to be constant throughout the period during which the model is applied.

Under these two assumptions, the only state variable of the system is mean dissolved oxygen concentrations and the only forcing variables are solar intensity and temperature.

The solar radiation at the surface of the water attenuates through the water column. The effective light intensity in the water column directly affects the phytoplankton population, which in turn, increases dissolved

oxygen during the day via photosynthesis and utilizes oxygen at night through respiration. Decaying phytoplankton, unconsumed fish feed and fish waste products also decrease DO as represented by sediment oxygen demand. The oxygen mass balance equations are specified by the program or calculated hourly over a 24 h period.

The rate of change in DO concentration in fishpond:

$$\frac{dDO}{dt} = P - C \pm E \quad (1)$$

P = DO production, C = DO Consumption, E = DO Exchanges

$$\frac{dDO}{dt} = DO_{ph} \pm DO_s - DO_{FR} - DO_{pr} - DO_{nr} - DO_{om} - DO_{sed} + DO_{in} - DO_{out} \quad (2)$$

$\frac{dDO}{dt}$ = Rate of change in DO concentration during the time interval, $gm^{-3} h^{-1}$.

dt = Rate of change in the time interval, h

DO_{ph} = Rate of photosynthetic production by phytoplankton, $g m^{-3} h^{-1}$.

DO_s = Rate of reaeration at the water surface, $g m^{-3} h^{-1}$.

DO_{FR} = Rate of DO respiration by fish, $g m^{-3} h^{-1}$.

DO_{pr} = Rate of DO respiration by phytoplankton, $g m^{-3} h^{-1}$.

DO_{nr} = Rate of DO consumption by nitrification, $g m^{-3} h^{-1}$.

DO_{om} = Rate of DO consumption by organic matter, $g m^{-3} h^{-1}$.

DO_{sed} = Rate of DO consumption by sediment, $g m^{-1} h^{-1}$.

DO_{in} = Rate of oxygen transfer with influent water, $g m^{-3} h^{-1}$.

DO_{out} = Rate of oxygen transfer with effluent water, $g m^{-3} h^{-1}$.

After calculating oxygen concentration for each element at each time step, the net oxygen change is then added to or subtracted from the previous time step's oxygen concentration. DO concentrations can be calculated at any time (t) as:

$$DO_t = DO_{t-1} + \left(\frac{dDO}{dt} \cdot dt \right) \quad (3)$$

DO_t = DO concentration (gm^{-3}) at time t

DO_{t-1} = DO concentration ($g m^{-3}$) at time t-1

2.1.1. Dissolved Oxygen Production:

- Photosynthetic dissolved oxygen production

In most aquaculture ponds phytoplankton provide the major source and sink for dissolved oxygen. Gross phytoplankton production rates are affected by many factors, including intensity of photosynthetically active radiation (PAR), light attenuation in the water column, water temperature.

Numerous expressions relating photosynthetic oxygen production are available (Eilers and Peeters, 1988). The rate of phytoplankton oxygen production can be calculated as (Smith, 1936 and Talling, 1957):

$$DO_{ph} = \frac{P_{max}}{KZ} \ln \left[\frac{E_z + \sqrt{\left(\frac{P_{max}}{\alpha}\right)^2 + E_z^2}}{E_z \exp(-KZ) + \sqrt{\left(\frac{P_{max}}{\alpha}\right)^2 + (E_z \exp(-KZ))^2}} \right] \quad (4)$$

where:

P_{max} = Maximum of DO production vs light curve ($g\ O_2m^{-3}\ h^{-1}$)

E_z = Light intensity at depth Z (Wm^{-2})

K = Light extinction coefficient (m^{-1})

Z = Depth of water (m)

α = Initial slope of the DO production vs light curve ($g\ O_2m^{-3}\ (W\ m^{-2})\ h^{-1}$).

Light intensity within the water column can be evaluated by Beer-Lambert law, where the light intensity is attenuated exponentially with depth. The light extinction coefficient is influenced by the absorption and scattering of light within the water column dissolved and suspended substances of biological and non-biological. Light intensity can be calculated from relationship:

$$E_z = E_t e^{-KZ} \quad (5)$$

E_t = Total solar radiation at water surface (Wm^{-2})

The total solar radiation flux incident (E_t) on a surface is the combination of the direct (subscript D), diffuse (subscript d) and ground-reflected (subscript r) irradiance of the surface which gives (ASHRAE, 2005):

$$E_t = E_D + E_d + E_r \quad (6)$$

The amount of solar irradiance is computed based on a number of solar angles and apparent solar time.

Apparent solar time (AST) is, in decimal hours:

$$AST = LST + \frac{ET}{60} + \frac{LSM - LON}{15} \quad (7)$$

where:

LST = local standard time, decimal hours

ET = equation of time, decimal minutes

LSM = local standard time meridian, decimal degrees.

LON = local longitude, decimal degree.

The equation of time as taken from **Duffie and Beckman (1991)** is:

$$ET = 229.2 \left\{ 0.000075 + 0.001868 \cos \left[(\eta - 1) \frac{360}{365} \right] - 0.032077 \sin \left[(\eta - 1) \frac{360}{365} \right] - 0.014615 \cos 2 \left[(\eta - 1) \frac{360}{365} \right] - 0.04089 \sin 2 \left[(\eta - 1) \frac{360}{365} \right] \right\} \quad (8)$$

Where: η is the number of the day from the first of January (where January 1st is $\eta=1$)

The solar altitude (β) can be calculated as:

$$\sin \beta = \cos L \cos \delta \cos H + \sin L \sin \delta \quad (9)$$

Where:

L = latitude angle, degrees

δ = solar declination angle, degrees

$$\delta = 23.45 \sin \left\{ \frac{[360(284 - \eta)]}{365} \right\} \quad (10)$$

H = solar hour angle, degrees

$$H = 15(AST - 12) \quad (11)$$

The solar incident angle (θ) can be computed as:

$$\cos \theta = \cos \beta \cos \gamma \sin \Sigma + \sin \beta \cos \Sigma \quad (12)$$

Where:

Σ = surface tilt angle from the horizontal plane, horizontal = 0°

γ = surface-solar azimuth angle

$$\gamma = \phi - \Psi \quad (13)$$

ϕ = solar azimuth angle

$$\cos \phi = \frac{\sin \beta \sin L - \sin \delta}{\cos \beta \cos L} \quad (14)$$

Ψ = surface azimuth angle, degrees

Now the equations of solar irradiance are computed based on all of these angles in the following manner. The surface direct irradiance:

$$\text{If } \cos \theta > 0 \xrightarrow{\text{then}} E_D = E_{DN} \cos \theta, \xrightarrow{\text{otherwise}} E_D = 0 \quad (15)$$

And where (E_{DN}) is the surface direct irradiance and is calculated as:

$$\text{If } \beta > 0 \xrightarrow{\text{then}} E_{DN} = \frac{A}{\text{EXP}\left(\frac{B}{\sin \beta}\right)}, \xrightarrow{\text{otherwise}} E_{DN} = 0 \quad (16)$$

The diffuse irradiance E_d

For vertical surfaces

$$E_d = CYE_{DN}$$

For surfaces other than vertical

$$E_d = CYE_{DN} \frac{(1+\cos\Sigma)}{2}$$

Where Y is the ratio of the sky diffuse irradiation on a vertical surfaces to the sky diffuse irradiation on a horizontal surfaces and

If $\cos(\theta) > -0.2$ $Y = 0.55 + 0.437 \cos(\theta) + 0.313 \cos^2(\theta)$, otherwise $Y = 0.45$

Finally, the ground-reflected irradiance E_r is computed as:

$$E_r = E_{DN}(C_n + \sin \beta)\rho_g \left(\frac{1 - \cos \Sigma}{2}\right) \quad (17)$$

where:

A = apparent solar radiation, W m^{-2}

$$= 1147.5868 + 57.4985 \times \sin(0.0174 \times \eta + 1.4782) \quad (18)$$

B = atmospheric extinction coefficient

$$= 0.1639 + 0.0237 \times \sin(0.0202 \times \eta + 4.013) \quad (19)$$

C = sky diffuse factor

$$= 0.1207 + 0.0179 \times \sin(0.0203 \times \eta + 3.9798) \quad (20)$$

C_n = clearness number

ρ_g = ground reflectivity, often taken to be 0.2 for typical mixture of ground surfaces.

- **Reaeration:**

Water surface reaeration can be either a source or a sink depending on the DO difference between the surface water and the air. A first order function is used to predict the reaeration rate (Culberson, 1993):

$$DO_S = K_{do}(C_s - DO_{surf})/Z \quad (21)$$

where:

K_{do} = oxygen transfer coefficient, $m\ h^{-1}$. It can be determined by (Banks and Herrera; 1977):

$$K_{do} = 0.0036(8.43 \times W_s)^{0.5} - 3.67 \times W_s + 0.43 \times W_s^2 \quad (22)$$

W_s = wind speed at two meter above the water surface, $m\ s^{-1}$.

C_s = saturated DO in water at a given elevation and temperature, $g\ m^{-3}$. It can be calculated by (Culberson, 1993):

$$C_s = (14.625 - 0.41(T_w) + 0.00799(T_w)^2 - 0.00778(T_w)^3) \times (1 - 0.0001E) \quad (23)$$

E = site elevation, m.

DO_{surf} = dissolved oxygen concentration for the surface layer, $g\ m^{-3}$.

T_w = water temperature, °C.

2.1.2. Dissolved oxygen Consumption:

In an aquaculture pond after sunrise, DO increases due to photosynthesis, but at night, biotic respiration and chemical oxidants result in a net loss of oxygen, which can reach critically, low concentrations. Loss of oxygen from fishpond is due to fish respiration, plankton respiration, water column respiration and sediment respiration.

- **Fish Respiration**

The rate of oxygen consumption through fish respiration ($mg\ O_2\ kg^{-1}\ h^{-1}$) can be calculated on water temperature and average fish weight. This calculation is shown in the following equation (Ali, 1999):

$$F_R = 2014.45 + 2.75 \times W_n - 165.2 \times T_w + 0.007 \times W_n^2 + 3.93 \times T_w^2 - 0.21 \times W_n \times T_w \quad (24)$$

$$DO_{FR} = F_R \times S_D / 1000 \quad (25)$$

where:

F_R = oxygen consumption through fish respiration mg O₂ kg⁻¹ h⁻¹,

W_n = average of individual fish weight, g,

S_d = stocking density, kg_{fish} m⁻³

- **Phytoplankton Respiration**

Respiration by phytoplankton and other microorganisms is a function of temperature as defined by Boyd *et al.* (1978):

$$DO_{PR} = -1.133 + 0.0038 \times SDD + 0.000014 \times SDD^2 + 0.081 \times T_w - 0.000749 \times T_w^2 - 0.00035 \times SDD \times T_w \quad (26)$$

SDD = Secchi disc depth (m)

- **Nitrification:**

Ammonia concentration represents the total ammonia nitrogen (TAN) from fertilizers and fish wastes. Nitrification is a two steps process where ammonia is oxidized to nitrite and then to nitrate. The oxygen consumption in nitrification process can be calculated as (Lee *et al.*, 1991):

$$DO_{NR} = 4.57 \times k_{NR} \times Nr / V \quad (27)$$

Where:

4.57 = stoichiometric coefficient for oxygen consumption in nitrification, gO₂ gTAN⁻¹.

$$k_{NR} = 0.1(1.08)^{(T_w-20)}$$

Nr = nitrification rate, gTAN h⁻¹.

$$Nr = 0.03 \times \frac{F_r \times W_n \times N_F}{24 \times 100} \quad (28)$$

F_r = Feeding Ratio, % of body fish day⁻¹

The feeding ratio can be calculated as (Ali, 1999):

$$F_r = 17.02 \times e^{\left[\frac{(\ln W_n + 1.14)^2}{-19.52}\right]} \quad (29)$$

where:

N_F = No. of fish

n = number of day from the start.

- **Oxidation of organic matter:**

The rate of oxidation of organic matter by bacteria is influenced by temperature and the function of temperature can be calculated as:

$$DO_{om} = \left[\frac{K_{om}}{1000} \times \theta^{(T_w - T_m)} \right] / Z \quad (30)$$

Where:

K_{om} = oxidation of organic matter rate at reference temperature, mg $O_2 m^{-2} h^{-1}$.

θ = temperature correction factor, 1.047 (Tetra Tech, 1980).

T_m = reference temperature, 20 °C.

- **Sediment Respiration Rate:**

Although there are many factors affecting sediment respiration, sediment respiration is described by a simple function which includes the influence temperature (Jamu, 1998). The model is expressed as (Culberson, 1993):

$$DO_{sed} = \left[\frac{K_{sed}}{1000} \times \theta^{(T_w - T_m)} \right] / Z \quad (31)$$

where:

K_{sed} = sediment respiration rate at reference temperature, mg $O_2 m^{-2} h^{-1}$.

θ = temperature correction factor, 1.065 (Culberson, 1993).

- **Dissolved oxygen in the influent and effluent water.**

The oxygen input to the surface layer is calculated as:

$$DO_{in} = Q_{in} \times DO_{inf} / V \quad (32)$$

where:

DO_{inf} = DO concentration in the influent water, g m^{-3} .

Q_{in} = influent water discharge, $m^3 h^{-1}$.

V = water volume, m^3 .

The oxygen output in the effluent water can be calculated as:

$$DO_{out} = Q_{out} \times DO_{surf} / V \quad (33)$$

Where:

DO_{surf} = DO concentration at the surface layer, g m^{-3} .

Q_{out} = effluent water discharge, $m^3 h^{-1}$.

2.2. Fish growth model.

The main objective for aquatic system is to increase the efficiency of fish growth. Fish growth is influenced not only by intrinsic factors such as fish size but also by a variety of environmental factors, including water temperature, photo-period, dissolved oxygen, unionized ammonia and food availability. These factors affect fish growth via their impacts on food consumption.

In order to calculate the daily growth rate “DGR” (g/day), for individual fish, the model developed by Yang Yi (1998) was used. It includes the main environmental factors influencing fish growth. Those factors are temperature, dissolved oxygen and unionized ammonia. The dissolved oxygen was generated from this model and the other water quality parameters was entered at the optimum levels for obtain the weight of individual fish throughout the year (Table 1).

$$DGR = (0.2914 \tau \kappa \delta \varphi h f W^m) - KW^n \tag{34}$$

Where:

- τ = temperature factor ($0 < \tau < 1$, dimensionless),
- κ = photoperiod factor ($0 < \kappa < 1$, dimensionless),
- δ = dissolved oxygen factor ($0 < \delta < 1$, dimensionless),
- φ = unionized ammonia (UIA) factor ($0 < \varphi < 1$, dimensionless),
- h = coefficient of food consumption ($g^{-1-m} day^{-1}$),
- f = relative feeding level ($0 < f < 1$, dimensionless), and
- K = coefficient of catabolism.

Cuenco et al. (1985) reported that food consumption was not affected when DO was above a critical limit (DO_{crit}); DO_{crit} decreased more or less linearly with decreasing DO levels until a minimum level (DO_{min}) was reached, below which fish would not feed. The function (δ) describing the effects of DO on food consumption was expressed by Bolte et al. (1995) as:

$$\delta = 1.0 \quad \text{if} \quad DO > DO_{critical}$$

$$\delta = \frac{DO - DO_{min}}{DO_{critical} - DO_{min}} \quad \text{if} \quad DO_{min} \leq DO \leq DO_{critical}$$

$$\delta = 0.0 \quad \text{if} \quad DO < DO_{min}$$

The DO_{crit} and DO_{min} used in the present model were 3.0 and 0.3 $g\ m^{-3}$, respectively (Yang Yi, 1998).

Ursin (1967) assumed that the coefficient of catabolism (K) increases exponentially with temperature. Nath et al. (1994) modified this exponential from to include the minimum temperature (assumed to be equivalent to T_{min}) below which the fish cannot survive as follow:

$$K = k_{min} \text{EXP} \{ j (T - T_{min}) \} \tag{35}$$

Where: k_{min} is the coefficient of fasting catabolism ($g^{1-n}\ day^{-1}$) at T_{min} , and j is the constant to describe temperature effects on catabolism.

Nath et al. (1994) used data on fasting Nile tilapia from Satoh et al. (1984) to estimate k_{min} and j to be 0.00133 and 0.0132, respectively.

The value of parameters ‘h’, ‘n’ and ‘m’ were assumed to be 0.80 (Bolte et al., 1995), 0.81 (Nath et al., 1994) and 0.67 (Ursin, 1967), respectively.

Table (1): Parameters used in Yang Yi model.

Parameter	Value	Reference
Photoperiod factor (κ)	1.0	Caulton (1982)
Temperature factor (τ)	1.0	Cuenco et al. (1985) Bolte et al. (1995) (Yang Yi, 1998)
Unionized ammonia factor (ϕ)	1.0	Colt and Armstrong (1981) Cuenco et al. (1985) Bolte et al. (1995) Abdalla (1989)
Coefficient of food consumption (h)	0.81	Bolte et al., (1995)
Relative feeding level (f)	0.37	Racoky, (1989)

Equation (34) is used to predict the daily growth rate. Equation (36) is used to calculate the accumulate growth starting by one gram of individual fish to the marketable weight of 250 grams.

$$W_n = W_{n-1} + DGR_n \tag{36}$$

3. Model Validation.

The developed dissolved oxygen model has been solved with the help of a computer program based on Excel software. To verify the accuracy of the developed model, experimental validations were conducted for a typical winter and summer days, 17th of January and 17th of July. The hourly variation of total solar radiation, dissolved oxygen, phytoplankton concentrations, temperature and secchi disc depth were used as inputs to calibrate the DO model. The coefficients and constants were used during model calibration are presented in Table 2.

Table 2: Model parameters used for computation:

Parameters	Value	Unit	Reference
Latitude	28.4	degree	This study
Longitude	30.0	degree	This study
Area (A_p)	400	m^2	This study
Depth (Z)	1.0	m	This study
No. of fish	1600	No.	This study
Weight of individual fish, W	1.0-250	g	This study
DO_{surf}	6.0	$g\ m^{-3}$	This study
SDD	0.37	M	This study
Initial slope (α)	0.0081	$gO_2\ m^{-3}\ (W\ m^{-2})\ h^{-1}$	Smith, 1936&Talling,1957
K	0.86	m^{-1}	Smith, 1936&Talling,1957
P_{max}	0.72	$gO_2\ m^{-3}\ h^{-1}$	Smith, 1936&Talling,1957
T_w	28		This study
Wind speed	N	$m\ s^{-1}$	This study
Initial DO	6.0	$g\ m^{-3}$	This study
K_{om}	1.08-3.00	$mg\ m^{-2}\ h^{-1}$	Jorgensen &Gromiec, 1989 Schroeder, 1987
K_{sed}	0.005-0.01	$mg\ m^{-2}\ h^{-1}$	Jamu, 1998

3.1 Solar Radiation:

The equations describing solar radiation are based in theoretical and experimental basis and it has been applied to calculate total solar radiation falling on fishpond water surface.

To verify the accuracy of the developed model, daily average global solar radiation data measured on the horizontal surface is compared with that theoretically computed on the same surfaces for the day average of typical winter (17th, January) day as revealed in figure (1), and summer (17th, July) day as shown in figure (2). It is observed that both the set of values are closely matched indicating that the developed model is validated well.

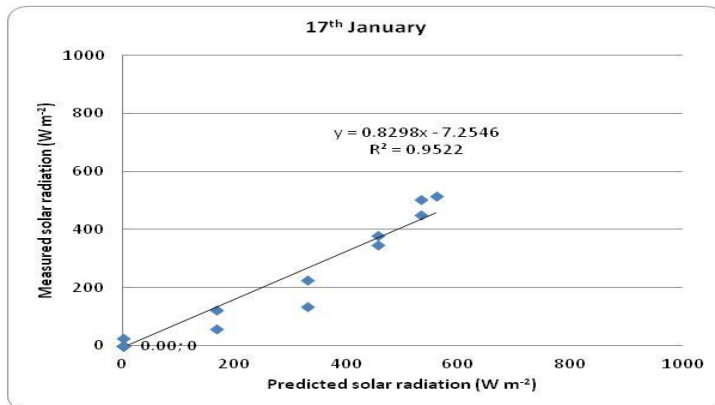


Fig.(1): Linear regression analysis of measured and predicted model solar radiation for the average day of January month.

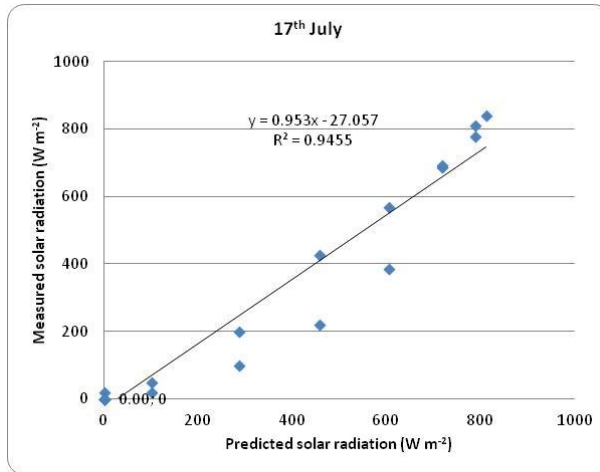


Fig. (2): Linear regression analysis of measured and predicted model solar radiation for the average day of July month.

3.2 Dissolved Oxygen.

The model runs utilizing input data from a 400m² tilapia production ponds at the World Fish Center, Regional Center for Africa and West Asia, Abbassa, AbouHammad, Sharkia, Egypt on typical summer (17th of July) day. The available data at this center were air temperature, wind speed and direction and water pond temperature recorded every five minutes. The model uses the first two parameters to predict water pond dissolved oxygen were compared to the measured values for model validation.

Correlation, Regression and Relative Percentage of Error, RPE, [(Actual – Prediction)/Actual, El-Haddad, 1977] were used as indicators of the level of agreement degree between the predicted and measured values.

The simulated dissolved oxygen was fluctuated between -0.101 to 0.113gO₂m⁻³ lower and higher than the measured dissolved oxygen for most of the 24-hour simulation (Figure 5). The RPE for the 24 hours of simulation was 0.2818% and the correlation coefficient between simulated and measured dissolved oxygen was 0.97.

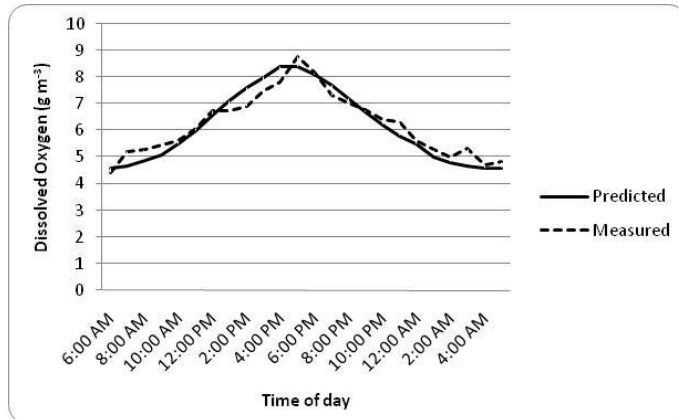


Figure (4): Measured and predicted dissolved oxygen.

The pond DO concentration was positively correlated with solar radiation and maximum production was at higher solar intensity. It increases as the phytoplankton produces more oxygen through photosynthesis than is consumed through respiration and decay. The phytoplankton photosynthesis decreases as the intensity of the solar radiation decreases in the late afternoon. Algae respond to the daily solar radiation and will reach their maximum rate of photosynthesis at a light intensity, which is a function of the daily solar radiation (Iohimura, 1960).

From the Fig. 4, it is noted that the DO reaches its maximum between 13:00 to 15:00 of sunshine hours, while the minimum values were observed at dawn. The hourly predictions of DO concentrations are close to the experimental values. The predicted DO exhibited agreement with the values of coefficient of correlation $r = 0.97$. In the morning hours the pond DO is falling due to the phytoplankton, fish respiration. Regression analysis was carried out between the measured and predicted DO, and the most appropriate form in the following equation:

$$\text{Predicted DO} = 1.046 + 0.837 \times \text{Measured DO}$$

The model output has correlation with the experimental data at a determination coefficient of (0.943). Such an agreement of the predicted model data and that of the actual experimental data indicate that the rates and constants used in the development of the model are valid for a description of the processes of utilization and production of DO (Fig. 5).

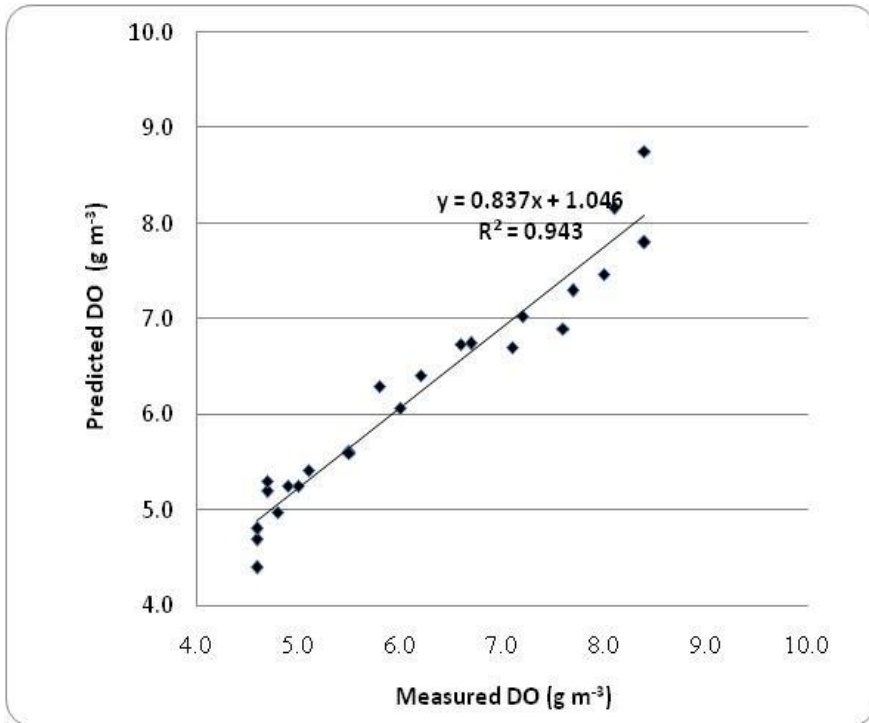


Fig.(5):Linear regression analysis of measured and predicted model DO for fishpond.

4. Model Application.

4.1. Oxygen production.

From the Fig. 4 it is seen that maximum solar radiation occurs at 12.00-13.00 h. The photosynthetic oxygen production is plotted against intensity of photosynthetically active radiation(PAR) of the pond during sunshine hours in Fig. 6. Regression analysis was carried out between the photosynthetic oxygen production and the intensity of photosynthetically active radiation(PAR), and the most appropriate form in the following equation:

$$\text{Photosynthetic oxygen production} = -0.642 + 0.239LN (PAR)$$

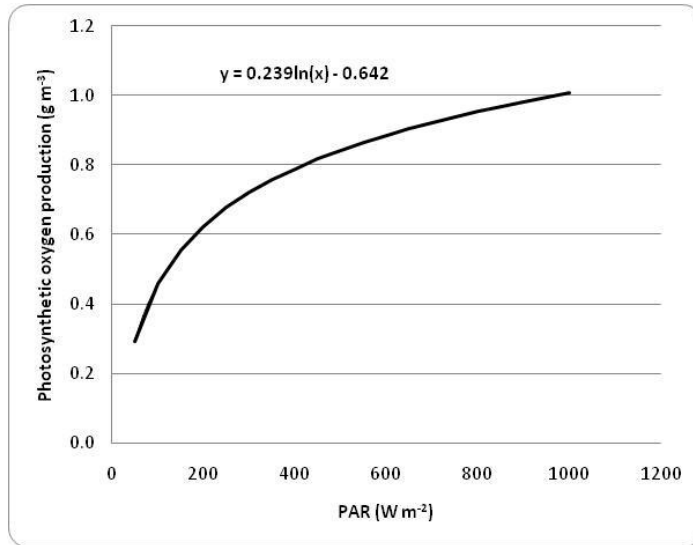


Fig. (6): Relation between photosynthetic oxygen production and photoactive solar radiation (PAR, W m⁻²) during sunshine hours

4.2. Fish Growth:

Figure (7) shows the hourly weight gain (gh⁻¹) and weights of individual fish (g) versus growing period (h). The results indicated that the total cycle time between the stocking and the harvesting is about 180-190 days; compared with the total cycle time in natural setting is about 210-240 days. These differences were probably due to differences in water quality with respect to both dissolved oxygen and total ammonia nitrogen.

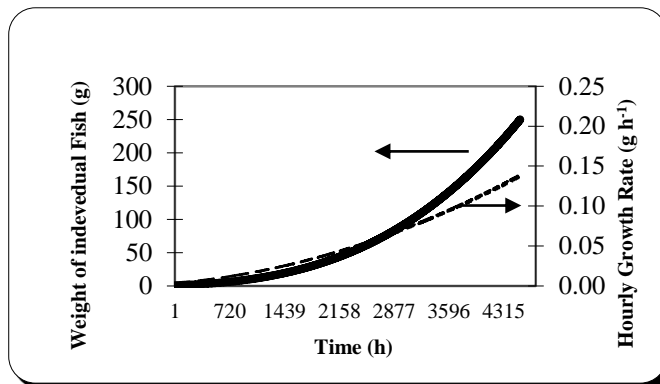


Figure (7): The weight of individual fish (g) and hourly weight gain (gh⁻¹) versus growing period (h) at temperature 28°C and unionized ammonia < 0.06 g m⁻³.

CONCLUSIONS:

A mass balance of the dissolved oxygen in 400 m³ earthen aquaculture ponds was carried out considering the factors affecting it such as temperature and solar intensity.

Components considered in the DO model include the production of DO by phytoplankton and reaeration and consumption of oxygen by phytoplankton, fish, organic matter, nitrification and sediment. Numerical equations were solved with computer model to predict DO in the pond. The amount and distribution of oxygen production in the water column depend on solar intensity and penetration as well as phytoplankton concentration.

The predicted results indicate that DO is affected by weather variables, especially solar radiation. The dissolved oxygen (DO) values ranged from 4.4 to 8.7 g m⁻³, where it reached the highest value (8.7) at 17:00 h, while it reached the lowest value (4.4) at 6:00 h.

Results from model verification runs showed that the model performance was satisfactory with respect to aquaculture pond dissolved oxygen. The relative percentage of error (RPE) for the 24 hours of simulation was 0.2818% and the correlation coefficient between predicted and measured dissolved oxygen was 0.97. The predicted dissolved oxygen was fluctuated between -0.101 to 0.113 g O₂ m⁻³ lower and higher than the measured dissolved oxygen for most of the 24 hour simulation.

The fish growth model results indicated that the total cycle time between the stocking and the harvesting is about 180-190 days during the summer months; compared with the total cycle time in natural setting is about 210-240 days.

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الملخص العربي**إتزان كتلي للأكسجين الذائب في أحواض الزراعة المائية**

سمير أحمد علي*

يعتبر الأكسجين الذائب في مياه أحواض الزراعة المائية من أهم محددات إنتاج الأسماك. لذلك فإن التنبؤ بتركيز الأكسجين الذائب في مياه أحواض الأسماك خلال العام من الأمور المهمة لتصميم وتخطيط الزراعات المائية.

وبناءً عليه فالهدف من هذه الدراسة هو تطوير نموذج للاتزان الكتلي للأكسجين الذائب للأحواض الأرضية في الزراعة المائية، الغرض منه:

- معرفة العوامل المؤثرة على إنتاج واستهلاك الأكسجين الذائب في أحواض الزراعة المائية.

- التنبؤ بتركيز الأكسجين الذائب في مياه تلك الأحواض.

ولهذا الغرض تم بناء برنامج حاسب آلي لحل المعادلة التفاضلية التالية:

$$\frac{dDO}{dt} = DO_{ph} \pm DO_s - DO_{FR} - DO_{pr} - DO_{nr} - DO_{om} - DO_{sed} + DO_{in} - DO_{out}$$

حيث:

$$\begin{aligned} \frac{dDO}{dt} &= \text{معدل التغير في تركيز الأكسجين الذائب عند وقت الحساب (جم أكسجين}^{-3}\text{ ساعة}^{-1}\text{)}, \\ \frac{dDO}{dt} &= \text{معدل التغير في الزمن (ساعة)}, \\ DO_{ph} &= \text{معدل إنتاج الأكسجين في البناء الضوئي للنباتات (جم أكسجين}^{-3}\text{ ساعة}^{-1}\text{)}, \\ DO_s &= \text{معدل إنتاج الأكسجين عن طريق التهوية عند سطح الماء (جم أكسجين}^{-3}\text{ ساعة}^{-1}\text{)}, \\ DO_{FR} &= \text{معدل استهلاك الأكسجين عن طريق الأسماك (جم أكسجين}^{-3}\text{ ساعة}^{-1}\text{)}, \\ DO_{pr} &= \text{معدل استهلاك الأكسجين عن طريق الهانمات النباتية (جم أكسجين}^{-3}\text{ ساعة}^{-1}\text{)}, \\ DO_{nr} &= \text{معدل استهلاك الأكسجين في عمليات النترة (جم أكسجين}^{-3}\text{ ساعة}^{-1}\text{)}, \\ DO_{om} &= \text{معدل استهلاك الأكسجين عن طريق المادة العضوية (جم أكسجين}^{-3}\text{ ساعة}^{-1}\text{)}, \\ DO_{sed} &= \text{معدل استهلاك الأكسجين عن طريق الرواسب (جم أكسجين}^{-3}\text{ ساعة}^{-1}\text{)}, \\ DO_{in} &= \text{معدل إنتقال الأكسجين مع الماء الداخل للحوض (جم أكسجين}^{-3}\text{ ساعة}^{-1}\text{)}, \\ DO_{out} &= \text{معدل إنتقال الأكسجين مع الماء الخارج من الحوض (جم أكسجين}^{-3}\text{ ساعة}^{-1}\text{)}. \end{aligned}$$

يلي ذلك حساب تركيز الأكسجين الذائب عند وقت ما كما يلي:

$$DO_t = DO_{t-1} + \left(\frac{dDO}{dt} \cdot dt \right)$$

حيث: DO_t = تركيز الأكسجين الذائب عند وقت ما t (جم أكسجين م⁻³).

*أستاذ الهندسة الزراعية المساعد - كلية الزراعة - جامعة بنها

$$\text{معدل التغير في تركيز الأكسجين الذائب عند وقت ما } t \text{ (جم أكسجين م}^{-3}\text{)} = \frac{dDO}{dt}$$

$$DO_{t-1} = \text{تركيز الأكسجين الذائب عند وقت } t - 1 \text{ (جم أكسجين م}^{-3}\text{)},$$

استخدمت بيانات المناخ المأخوذة من خلال محطة الأرصاد بالمركز الدولي للأسمك بالعباسة محافظة الشرقية، وذلك للتنبؤ بتركيز الأكسجين الذائب في مياه الأحواض خلال العام.

وكانت أهم النتائج هي أن أكثر العناصر تأثيراً على إضافة أكسجين ذائب للمياه هي عملية البناء الضوئي للهائمات النباتية (0.25- 1.00 جم أكسجين م⁻³) بناءً على شدة الإشعاع الشمسي. وكان أكثر العناصر إستهلاكاً للأكسجين هو تنفس الأسماك.

بعد ذلك تم تجريب النموذج باستخدام تركيز الأكسجين الذائب المنتبأ به في النموذج الحالي في نموذج Yang Yi, 1998 للحصول على الزيادة اليومية في وزن السمكة، وبالتالي معرفة المدة التي يتم فيها الوصول إلى الحجم التسويقي للأسماك في حالة توفر الظروف المثلى لعوامل جودة المياه الأخرى مثل درجة حرارة المياه والأمونيا وغيرها. وهذه الخطوة تمكن العاملين في هذا المجال بعمل إستراتيجية للإنتاج طوال العام وكانت أهم النتائج كما يلي:

- أوضحت نتائج اختبار الصلاحية أن معدل أداء النموذج مرضياً بدرجة كافية للتنبؤ بتركيز الأكسجين الذائب في المياه، حيث كان الارتباط بين البيانات المنتبأ بها والمقاسة 97%، كما أن الخطأ النسبي خلال 24 ساعة لا يتعدى 0.2818%، وكان تركيز الأكسجين الذائب المنتبأ به يتراوح بين 0.101 و 0.113 (جم أكسجين م⁻³) أقل وأعلى من تركيز الأكسجين الذائب المقاس خلال 24 ساعة.

- كانت أهم نتائج نموذج نمو الأسماك هي أنه يمكن الوصول إلى الوزن التسويقي (250 جم) خلال 180-190 يوم خلال أشهر الصيف، في حين أنه في الطبيعة نصل إلى الحجم التسويقي خلال 210-240 يوم ويرجع هذا الاختلاف إلى أننا استخدمنا في النموذج العوامل البيئية المثلى وهو ما لم يتوفر في الطبيعة.